

## GENERAL THERMODYNAMICS

## Problem Set 1

Due: September 20, 1990

1. Which of the following systems are the same ?
  - (a) An amount of 1 kg of water in a cylinder with an adjustable piston is in a gravitational field. The volume of the cylinder varies from 0 to  $1 \text{ m}^3$ , and the field from 0 to 1 g.
  - (b) An amount of 1 kg of water is confined in a vessel of volume  $1 \text{ m}^3$ . The vessel is in a gravitational field of 1 g.
  - (c) An amount of 1 kg of water in a cylinder with an adjustable piston as in (a) is in a spacecraft orbiting the earth.
  - (d) An amount of 1 kg of water in a cylinder with an adjustable piston as in (a) is in a spacecraft commuting between the surface of the earth and an orbit.
  - (e) An amount of 1 kg of water in a cylinder with an adjustable piston as in (a) is in a spacecraft commuting between the surface of Jupiter and an orbit.
  - (f) An amount of water between 0 and 1 kg in a cylinder with an adjustable piston as in (a) is in a gravitational field that varies from 0 to 1 g.
  
2. At a given point in time, system A consists of 10 water molecules,  $\text{H}_2\text{O}$ , in a vessel, system B consists of 10 hydrogen molecules,  $\text{H}_2$ , and 10 oxygen atoms, O, in a vessel identical to that of A, and system C consists of 100 water molecules in a vessel identical to that of A.
 

Are systems A, B and C completely defined ? If yes, are they identical ? If no, define them such that systems A, B and C are identical.
  
3. Consider a system consisting of a water molecule in a rigid container. Which of the following are properties of the system?
 

<ol style="list-style-type: none"> <li>(a) The position of the molecule.</li> <li>(c) The path of the molecule between two points in time.</li> </ol>	<ol style="list-style-type: none"> <li>(b) The speed of the molecule.</li> <li>(d) The interaction with another system needed to accelerate the molecule from a lower to a higher speed.</li> </ol>
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4. Problem 2.10
5. What is the difference between a property and a state ?
6. Problem 3.6
7. Problem 3.17

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**Problem Set 2**

**Due: September 27, 1990**

1. In the tutorial session on September 18, the two following issues remained unresolved:
  - (a) Are friction forces internal or external? Think about your answer (s) carefully.
  - (b) The constituents of a system are billiard balls identical in every respect except that each ball has either a stripe or uniform colour. Is each kind of ball a different constituent? Justify your answer(s).
2. Problem 3.26
3. Problem 4.6
4. Problem 4.9
5. Problem 5.4
6. Problem 3.27. It will not be graded, but you are encouraged to work it and hand it in for your own edification.

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**Problem Set 3**

**Due: October 4, 1990**

1. Problem 3.24
2. Problem 6.1
3. A well-insulated water tank in state 1 is filled with hot water on top and cold water at the bottom. In state 2, the water in the tank is in a stable equilibrium state with the same energy as in state 1. In all states considered in this problem, the volume of the tank and the amount of water in it are the same.
  - (a) What kind of state is state 1 ?
  - (b) If the water in the tank in state 2 is connected with a reservoir R through cyclic machinery, energy can be transferred to a weight in a reversible process in the amount of 240 MJ . What are the adiabatic availability and the available energy with respect to reservoir R of state 2 ?
  - (c) If the tank in state 1 is connected to reservoir R through cyclic machinery, energy can be transferred to a weight in a reversible process in the amount of 300 MJ . What is the available energy with respect to reservoir R of the tank in state 1 ?
  - (d) State 3, a stable equilibrium state, is reached by a reversible process from state 1. If the tank in state 3 is connected to reservoir R through cyclic machinery, energy can be transferred to a weight in a reversible process in the amount of 120 MJ. What is the adiabatic availability of state 1 ?
  - (e) The price for 1 MJ of energy that can be transferred to a weight is 10 cents. How much money is lost if the tank is allowed to change from state 1 to state 2 ?
4. Problem 6.7
5. Problem 7.1
6. Problem 7.3

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Problem Set 4

Due: October 11, 1990

1. Problem 8.3
2. Problem 8.4
3. Problem 9.2
4. Problem 9.3
5. Problem 9.4

Elias:

- Could you please propose Problem Set 5?
- Farid will give you the solution to Problem Set 4 for review.
- I will be back on Monday, October 15, 1990.

Sincerely,



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Problem Set 5

Due: October 18, 1990

1. Problem 11.1
2. Problem 11.4
3. Problem 12.2

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Midterm Examination I

October 18, 1990

Problem 1 (30/100)

System A consists of only one constituent, and has only volume  $V$  as a parameter.

In stable equilibrium state  $A_1$ , the system has

<u>Energy</u>	<u>Volume</u>	<u>Amount of constituent</u>
$E_1 = 2.4 \times 10^5 \text{ J}$	$V_1 = 2.4 \times 10^{-6} \text{ m}^3$	$n_1 = 24 \text{ mol}$

Around state  $A_1$ , the fundamental relation can be accurately represented by the expression

$$S = 100(E V n)^{1/3}$$

where  $S$  is in J/K for  $E$  in J,  $V$  in  $\text{m}^3$ , and  $n$  in mol.

- (5/100) a. Find the entropy  $S_1$  of A in state  $A_1$ .
- (15/100) b. Find the temperature  $T_1$ , the pressure  $p_1$ , and the chemical potential  $\mu_1$  of A in state  $A_1$ .
- (5/100) c. Write a relation between small changes in energy, entropy, volume, and amount of the constituent from one to another stable equilibrium state.
- (5/100) d. Consider a stable equilibrium state  $A_2$  that has energy  $E_2$ , entropy  $S_2 = 240 + 10 \text{ J/K}$ , volume  $V_2 = 2.4 \times 10^{-6} + 1.2 \times 10^{-7} \text{ m}^3$ , and amount of the constituent  $n_2 = 24 + 0.5 \text{ mol}$ . Estimate the difference in energies  $E_2 - E_1$  using the result in part (c).

Problem 2 (35/100)

Consider two large, rigid tanks A and B. Tank A is filled with  $m_v = 5000$  kg of a vapor at  $700^\circ\text{C}$ , and tank B with  $m_g = 10,000$  kg of a gas at  $400^\circ\text{C}$ . For the stable equilibrium states of interest in this problem, the energy and entropy of either the vapor or the gas can be written as  $E = mc(T - T_0)$  and  $S = mc \ln(T/T_0)$ , where for the vapor  $c_v = 1.8$  kJ/kg K and for the gas  $c_g = 1.2$  kJ/kg K, and  $T_0$  is a constant expressed in kelvin.

Energy can be transferred to a weight from the composite of the rigid tanks by using a thermoelectric generator to power a motor.

- (15/100) a. What is the largest amount of energy that can be transferred to the weight in a weight process for the composite of A and B?
- (10/100) b. If in an irreversible weight process for the composite of A and B, the two systems A and B end in mutual stable equilibrium, and the weight receives half as much energy as in the weight process in part (a), how much entropy is generated by irreversibility in both A and B?
- (10/100) c. Considering your result in part (b), can you tell what fraction of the entropy generated by irreversibility is generated in A and what fraction in B? State your answer in a few lines.



Problem 3 (35/100)

Four states  $A_0, A_1, A_2, A_3$  of system A correspond to the same values of amounts of constituents and parameters. In addition, all states of reservoir R correspond to fixed values of amounts of constituents and parameters.

In state  $A_0$  system A has energy  $E_0 = 0$ , and is in mutual stable equilibrium with R. In addition, measurements yield the following results.

$$(a) \quad [W_{10}^{AR \rightarrow}]_{\text{rev}} = 70 \text{ kJ}$$

$$(b) \quad [W_{20}^{AR \rightarrow}]_{\text{rev}} = [W_{20}^{A \rightarrow}]_{\text{rev}} = 40 \text{ kJ}$$

$$(c) \quad [W_{30}^{AR \rightarrow}]_{\text{rev}} = 20 \text{ kJ}$$

$$(d) \quad [W_{12}^{A \rightarrow}]_{\text{irr}} = 0 \quad \text{and} \quad (S_{12})_{\text{irr}} = 0.1 \text{ kJ/K}$$

$$(e) \quad [W_{13}^{A \rightarrow}]_{\text{irr}} = 0$$

- (15/100) (a) What are the values of the energies  $E_1, E_2,$  and  $E_3$  of system A ?
- (10/100) (b) What is the temperature of the reservoir  $T_R$  ?
- (10/100) (c) How much entropy is generated by irreversibility in the course of the irreversible weight process from  $A_1$  to  $A_3$  ?

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Solution, Midterm Examination, 10/18/90

Problem 1

a.  $S_i = 100 (2.4 \times 10^5 \times 24 \times 10^{-6} \times 24)^{1/3} = 240 \text{ J/K}$ .

b.  $E = \left(\frac{S}{100}\right)^3 \frac{1}{Vn}$

$$\left(\frac{\partial E}{\partial S}\right)_{V,n} = \frac{3S^2}{10^6} \frac{1}{Vn} \quad T_1 = \frac{3 \times 240^2}{10^6} \frac{1}{2.4 \times 10^{-6} \times 24}$$
$$= 3000 \text{ K}$$

$$\left(\frac{\partial E}{\partial V}\right)_{S,n} = -\left(\frac{S}{100}\right)^3 \frac{1}{V^2 n} \quad p_1 = \frac{(2.4)^3}{(2.4 \times 10^{-6})^2 \times 24} =$$

$$= 10^{11} \frac{\text{N}}{\text{m}^2}$$

$$\left(\frac{\partial E}{\partial n}\right)_{S,V} = -\left(\frac{S}{100}\right)^3 \frac{1}{Vn^2} \quad \mu_1 = -\frac{(2.4)^3 \text{m}^3}{2.4 \times 10^{-6} \times 24^2}$$

$$= -10^4 \text{ J/mol}$$

c.  $dE = \left(\frac{\partial E}{\partial S}\right)_{V,n} dS + \left(\frac{\partial E}{\partial V}\right)_{S,n} dV + \left(\frac{\partial E}{\partial n}\right)_{S,V} dn$

$$= TdS - pdV + \mu dn$$

d.  $dE = E_2 - E_1 = T_1 dS - p_1 dV + \mu_1 dn$

$$= 3000 \times 10 - 10^{11} \times 1.2 \times 10^{-7} - 10^4 \times 0.5$$

$$= 1.3 \times 10^4 \text{ J}$$

## Problem 2

a. The largest energy is transferred to the weight when the process is reversible and A and B end in mutual stable equilibrium, i.e., temperature equality

The entropy balance is

$$m_v c_v \ln \frac{T_f^A}{T_i^A} + m_g c_g \ln \frac{T_f^B}{T_i^B} = 0 \quad T_f^A = T_f^B = T_2$$

$$5000 \times 1.8 \ln \frac{T_2}{973} + 10000 \times 1.2 \ln \frac{T_2}{673} = 0$$

$$T_2 = 673^{\frac{4}{7}} \times 973^{\frac{3}{7}} = 788 \text{ K} = \underline{515^\circ \text{C}}$$

So the energy balance yields

$$\begin{aligned} (W_{if}^{AB \rightarrow})_{rev} &= -m_v c_v (T_2 - T_i^A) - m_g c_g (T_2 - T_i^B) \\ &= -9000(515 - 700) - 12000(515 - 400) \\ &= \underline{285000 \text{ kJ} = 285 \text{ MJ}} \end{aligned}$$

b. Here the energy balance is

$$\frac{285000}{2} = -9000(T_2' - 700) - 12000(T_2' - 400)$$

$$21T_2' = 10960 \quad T_2' = 522^\circ \text{C} = 795 \text{ K}$$

For this temperature, the entropy balance yields

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**Problem Set 6**

**Due: October 25, 1990**

1. Problem 11.2
2. Problem 11.3
3. Problem 12.7

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## Problem Set 8

Due: November 8, 1990

1. Problem 17.4
2. Consider a simple system that has the surface area,  $a$ , as the only parameter, as it was introduced in Problem 17.4. In addition, it is specified that the system has only one constituent, whose amount is constant. The variation of the surface tension with temperature  $T$  for this system is given by  $\sigma = \sigma(T) = 7 \times 10^{-2} \text{ N m}^{-1} - 10^{-4} \text{ N (mK)}^{-1} (T - 273.15 \text{ K})$ . At a constant temperature of  $T_0 = 400 \text{ K}$ , the surface area of the system increases from  $a_1 = 1 \text{ m}^2$  to  $a_2 = 2 \text{ m}^2$ .
  - (a) Find the Maxwell relation that follows from the Helmholtz free energy for this system.
  - (b) What is the change in the entropy of the system for this constant-temperature process?
  - (c) What is the change in the internal energy of the system?
  - (d) What is the work that must be performed on the system if the process is reversible and the system experiences no work interactions other than through the change of surface area? (Hint: What is the work for a reversible constant-temperature process of a system that has volume as the only parameter?)
3. Problem 19.7
4. Problem 19.19
5. Problem 19.29

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General Thermodynamics

Midterm Examination II  
November 20, 1990

Problem 1 (30/100)

A heat engine interacts with two reservoirs  $R_1$  and  $R_2$ , at temperatures  $T_1$  and  $T_2$  ( $T_1 > T_2$ ). The work done by the engine is used to drive a heat pump which interacts with reservoirs  $R_2$  and  $R_3$ , at temperatures  $T_2$  and  $T_3$  ( $T_3 < T_2$ ).

- (15/100) a. If it is desired to transfer as much energy as possible out of reservoir  $R_3$ , and to use as little energy as possible out of reservoir  $R_1$ , what is the largest value of the ratio of these two energies? Express your answer in terms of  $T_1$ ,  $T_2$ , and  $T_3$ .
- (15/100) b. For  $T_1 = 900$  K,  $T_2 = 300$  K, and  $T_3 = 200$  K, it is found that the ratio of the energies out of  $R_3$  and  $R_1$  is equal to unity, and that the heat engine operates reversibly. How much entropy is generated by irreversibility per unit of energy exchanged by reservoir  $R_1$ ?

Problem 2 (30/100)

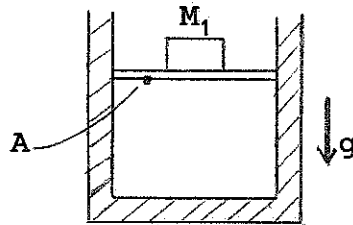
Consider two systems A and B. System A consists of 4.5 kg of air contained in a cylinder with a frictionless and massless piston of cross sectional area  $0.01 \text{ m}^2$ . The air behaves as a perfect gas with  $R_M = 287 \text{ J/kg K}$  and  $c_p = 1 \text{ kJ/kg K}$ , and is initially at temperature  $T_1^A = 4^\circ\text{C}$ . On top of the piston there is a mass  $m_w = 700 \text{ kg}$ . System B consists of a metal block. Its heat capacity  $C_B = 10 \text{ kJ/K}$ , and its initial temperature  $T_1^B = 120^\circ\text{C}$ .

- (15/100) a. Upon interacting with each other and the mass in the earth's gravity, the air and the metal block reach mutual stable equilibrium. How much energy is exchanged between the air and the block, and how much entropy is generated by irreversibility?
- (15/100) b. If cyclic machinery were interposed between the air with the weighted piston and the block, what is the largest work that can be done by the machinery?



Problem 3 (40/100)

In a well-insulated cylinder, a well-insulated, massless piston can move without friction. The area of the piston  $A = 1 \text{ m}^2$ , and on top of the piston lies a mass  $M_1 = 10,135 \text{ kg}$ . The piston is in a gravity field along the axis of the cylinder of  $g = 10 \text{ m/s}^2$ . Vacuum prevails outside of the cylinder.



The substance within the cylinder is initially in a stable equilibrium state 1. Then an additional mass  $M_2 = 9718 \text{ kg}$  is placed on top of the cylinder and, as a result, the system reaches a new stable equilibrium state 2. Determine state 2 if no entropy is generated, and the compressed substance is:

- (15/100) a. a monatomic perfect gas with a molecular weight  $M = 4 \text{ kg/kmol}$  at an initial temperature  $T_1 = 100^\circ\text{C}$ . What are the temperature  $T_2$  and specific volume  $v_2$  in state 2? The universal gas constant is  $R = 8.314 \text{ J/mol K}$ .
- (10/100) b. a two-phase mixture of water vapor and liquid water with an initial quality  $x_1 = 0.5$ . What are the temperature  $T_2$  and quality  $x_2$  in state 2? Water properties are attached.
- (15/100) c. a two-phase mixture of solid and liquid aluminum at  $T_1 = 660.4^\circ\text{C}$ . If state 2 consists of the same two phases as state 1, what is an estimate of the temperature  $T_2$ ? For aluminum at 1 bar,  $h_{jf} = 3.73 \times 10^5 \text{ J/kg}$  and  $v_{jf} = 2.625 \times 10^{-5} \text{ m}^3/\text{kg}$ .

TABLE B.14. Values of properties of water, H<sub>2</sub>O.<sup>a</sup>  
Properties of saturated H<sub>2</sub>O

<i>T</i>	<i>p</i>	<i>v<sub>f</sub></i>	<i>v<sub>g</sub></i>	<i>u<sub>f</sub></i>	<i>u<sub>gf</sub></i>	<i>u<sub>g</sub></i>	<i>h<sub>f</sub></i>	<i>h<sub>fg</sub></i>	<i>h<sub>g</sub></i>	<i>s<sub>f</sub></i>	<i>s<sub>fg</sub></i>	<i>s<sub>g</sub></i>
°C	kPa	m <sup>3</sup> /kg		kJ/kg			kJ/kg			kJ/kg K		
0.01	0.61133	0.0009997	206.14	0.0	2374.9	2374.9	0.0	2500.9	2500.9	0.0	9.1555	9.1555
5	0.87210	0.0009999	147.12	20.4	2361.4	2381.8	20.4	2489.7	2510.1	0.0741	8.9508	9.0249
10	1.2276	0.0010004	106.38	41.1	2347.6	2388.7	41.1	2478.2	2519.3	0.1478	8.7522	8.9000
15	1.7051	0.0010011	77.926	62.0	2333.6	2395.6	62.0	2466.5	2528.5	0.2207	8.5598	8.7806
20	2.3385	0.0010021	57.791	82.9	2319.6	2402.5	82.9	2454.7	2537.6	0.2928	8.3736	8.6664
25	3.1691	0.0010032	43.360	103.9	2305.4	2409.3	103.9	2442.8	2546.7	0.3640	8.1932	8.5571
30	4.2460	0.0010046	32.894	125.0	2291.1	2416.1	125.0	2430.8	2555.8	0.4341	8.0184	8.4525
35	5.6280	0.0010062	25.216	146.1	2276.8	2422.9	146.1	2418.7	2564.8	0.5032	7.8491	8.3523
40	7.3836	0.0010080	19.523	167.3	2262.4	2429.7	167.3	2406.6	2573.8	0.5712	7.6850	8.2562
45	9.5932	0.0010100	15.258	188.4	2248.0	2436.4	188.4	2394.4	2582.7	0.6381	7.5259	8.1640
50	12.349	0.0010121	12.032	209.5	2233.5	2443.0	209.5	2382.1	2591.6	0.7039	7.3716	8.0755
60	19.940	0.0010170	7.6710	251.6	2204.6	2456.2	251.6	2357.5	2609.1	0.8323	7.0764	7.9088
70	31.188	0.0010227	5.0422	293.7	2175.4	2469.1	293.7	2332.7	2626.4	0.9567	6.7978	7.7545
80	47.389	0.0010289	3.4072	335.6	2146.1	2481.7	335.7	2307.5	2643.2	1.0772	6.5342	7.6114
90	70.138	0.0010359	2.3606	377.5	2116.6	2494.1	377.6	2282.1	2659.6	1.1942	6.2841	7.4782
100	101.35	0.0010434	1.6729	419.4	2086.6	2506.1	419.5	2256.1	2675.6	1.3080	6.0460	7.3540
110	143.27	0.0010516	1.2102	461.4	2056.3	2517.6	461.5	2229.5	2691.0	1.4189	5.8189	7.2379
120	198.53	0.0010604	0.89186	503.5	2025.3	2528.8	503.7	2202.1	2705.8	1.5275	5.6013	7.1288
130	270.09	0.0010699	0.66851	545.8	1993.6	2539.4	546.1	2173.9	2720.0	1.6338	5.3923	7.0261
140	361.29	0.0010800	0.50885	588.4	1961.2	2549.6	588.8	2144.6	2733.4	1.7381	5.1910	6.9291
150	475.84	0.0010907	0.39278	631.2	1927.8	2559.1	631.8	2114.2	2746.0	1.8406	4.9964	6.8370
160	617.82	0.0011022	0.30706	674.4	1893.5	2567.9	675.1	2082.5	2757.6	1.9415	4.8079	6.7493
170	791.66	0.0011144	0.24282	718.0	1858.0	2576.0	718.8	2049.4	2768.2	2.0409	4.6246	6.6655
180	1002.1	0.0011275	0.19404	761.8	1821.4	2583.2	763.0	2014.7	2777.7	2.1388	4.4461	6.5849
190	1254.4	0.0011414	0.15653	806.1	1783.5	2589.5	807.5	1978.4	2785.9	2.2354	4.2716	6.5070
200	1553.8	0.0011564	0.12735	850.7	1744.1	2594.8	852.5	1940.2	2792.7	2.3308	4.1006	6.4314
210	1906.2	0.0011724	0.10441	895.7	1703.3	2599.0	897.9	1900.1	2798.0	2.4249	3.9326	6.3576
220	2317.8	0.0011897	0.086186	941.1	1660.7	2601.9	943.9	1857.7	2801.6	2.5181	3.7671	6.2852
230	2794.8	0.0012084	0.071577	987.1	1616.3	2603.4	990.4	1813.0	2803.4	2.6104	3.6033	6.2137
240	3344.2	0.0012287	0.059760	1033.5	1569.9	2603.4	1037.7	1765.6	2803.3	2.7020	3.4408	6.1428
250	3972.9	0.0012509	0.050123	1080.7	1521.1	2601.8	1085.7	1715.3	2801.0	2.7932	3.2788	6.0720
260	4688.5	0.0012753	0.042202	1128.7	1469.8	2598.5	1134.7	1661.6	2796.3	2.8843	3.1167	6.0009
270	5498.6	0.0013023	0.035641	1177.7	1415.4	2593.1	1184.8	1604.3	2789.1	2.9755	2.9536	5.9291
280	6411.6	0.0013323	0.030168	1227.8	1357.7	2585.5	1236.3	1542.6	2778.9	3.0672	2.7888	5.8560
290	7435.9	0.0013659	0.025568	1279.3	1296.1	2575.4	1289.4	1476.1	2765.5	3.1599	2.6212	5.7811
300	8580.9	0.0014040	0.021673	1332.3	1230.0	2562.4	1344.4	1403.9	2748.3	3.2539	2.4495	5.7034
310	9856.4	0.0014479	0.018349	1387.3	1158.5	2545.8	1401.6	1325.0	2726.6	3.3496	2.2722	5.6219
320	11274	0.0014991	0.015486	1444.6	1080.3	2524.9	1461.5	1237.9	2699.4	3.4479	2.0871	5.5350
330	12845	0.0015606	0.012996	1504.9	993.4	2498.3	1524.9	1140.3	2665.2	3.5499	1.8906	5.4405
340	14586	0.0016373	0.010797	1569.3	894.6	2463.9	1593.2	1028.2	2621.4	3.6576	1.6769	5.3345
350	16513	0.0017396	0.0088132	1640.5	777.2	2417.8	1669.3	894.0	2563.3	3.7754	1.4347	5.2101
360	18651	0.0018942	0.0069457	1725.0	625.9	2350.9	1760.4	720.1	2480.4	3.9142	1.1373	5.0515
370	21027	0.0022178	0.0049282	1847.9	380.3	2228.1	1894.5	437.2	2331.7	4.1167	0.6798	4.7965
374.14	22089	0.0031550	0.0031550	2029.1	0.0	2029.1	2098.8	0.0	2098.8	4.4289	0.0000	4.4289

<sup>a</sup>Data generated using the correlations in W. C. Reynolds, *Thermodynamic Properties in SI*, Dept. of Mech. Eng., Stanford University, Stanford, CA, 1979.

2.451J and 22.571J  
 Solution midterm examination, 11/20/90

Problem 1

a.

$$W_{h.e.}^{\rightarrow} = \left(1 - \frac{T_2}{T_1}\right) Q_1^{\rightarrow} - T_2 (S_{irr})_{h.e.}$$

$$Q_3^{\rightarrow} = \frac{T_3}{T_2 - T_3} W_{h.p.}^{\leftarrow} - \frac{T_2 T_3}{T_2 - T_3} (S_{irr})_{h.p.}$$

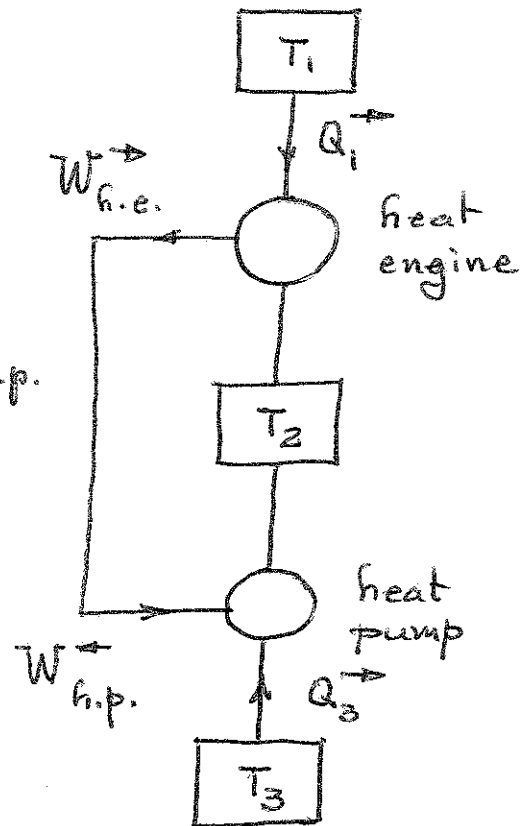
$$W_{h.e.}^{\rightarrow} = W_{h.p.}^{\leftarrow}$$

For the optimum ratio, the heat engine and the heat pump must be reversible. So

$$\left(\frac{Q_3^{\rightarrow}}{Q_1^{\rightarrow}}\right)_{opt} = \frac{1 - \frac{T_2}{T_1}}{\frac{T_2}{T_3} - 1} = \frac{1 - (1/3)}{(3/2) - 1} = \frac{4}{3}$$

b. When the heat engine is reversible, and the heat pump irreversible,

$$\frac{Q_3^{\rightarrow}}{Q_1^{\rightarrow}} = 1 = \frac{T_3}{T_2 - T_3} \cdot \left(1 - \frac{T_2}{T_1}\right) - \frac{T_2 T_3}{T_2 - T_3} (S_{irr})_{h.p.} \frac{1}{Q_1^{\rightarrow}}$$



$$\text{So } \frac{T_2 (\dot{S}_{\text{irr}})_{\text{h.p.}}}{\dot{Q}_1} = 1 - \frac{T_2}{T_1} - \frac{T_2 - T_3}{T_3} = 1 - \frac{1}{3} - \frac{3}{2} + 1 = \frac{1}{6}$$

$$\text{or } (\dot{S}_{\text{irr}})_{\text{h.p.}} / \dot{Q}_1 = 1/6 \times 300 = \underline{1/1800 \text{ K}^{-1}}$$

## Problem 2

The weight on top of A maintains a constant pressure  $p_1$ . So the change in energy of A plus the work done on the weight equals

$$\begin{aligned} m_A c_v (T_2^A - T_1^A) + p_1 (V_2^A - V_1^A) &= m_A (c_v + R) (T_2^A - T_1^A) \\ &= m_A c_p (T_2^A - T_1^A) \quad \text{because } pV = mRT \text{ for the} \\ &\text{gas in A. The energy balance yields} \end{aligned}$$

$$m_A c_p (T_2^A - T_1^A) + C_B (T_2^B - T_1^B) = -W_{\text{machinery}}^{\rightarrow}$$

and the entropy balance

$$m_A c_p \ln(T_2^A / T_1^A) + C_B \ln(T_2^B / T_1^B) = \dot{S}_{\text{irr}}$$

a. At mutual stable equilibrium  $T_2^A = T_2^B = T_2$ ,  $W^{\rightarrow} = 0$  (no machinery). So the energy balance yields

$$T_2 = \frac{m_A c_p T_1^A + C_B T_1^B}{m_A c_p + C_B} = \underline{84^\circ \text{C}}$$

The energy transfer out of the block is 360 kJ

and the entropy balance yields  $S_{irr} = 0.18 \text{ kJ/kg K}$ .

b. For largest work, again  $T_2^A = T_2^B = T_2$  but  $S_{irr} = 0$

So the entropy balance yields

$$T_2 = \left[ (T_1^A)^{m_A c_p} (T_1^B)^{C_D} \right]^{1/(m_A c_p + C_D)} = 352.6 \text{ K}$$
$$= \underline{79^\circ \text{C}}$$

and the energy balance

$$W_{\text{machinery}}^{\rightarrow} = \underline{72.5 \text{ kJ}}$$

### Problem 3

a. The gas constant of the substance is

$$R_M = R/M = 8.314 \text{ (kJ/kmol K)} / 4 \text{ (kg/kmol)}$$
$$= 2.079 \text{ kJ/kg K}$$

For isentropic compression

$$v_2 = v_1 \left( \frac{p_1}{p_2} \right)^{1/\gamma}$$

where  $v_1 = R_M T_1 / p_1$  and  $\gamma = \frac{5}{3} = 1.667 = \frac{c_p}{c_v}$

Moreover

$$\underline{T_2 = T_1 \left( \frac{p_1}{p_2} \right)^{-(\gamma-1)/\gamma}}$$

$$\text{So } v_2 = \frac{2079 \times 373.15}{1.014 \times 10^5} \times \left( \frac{1.014}{1.985} \right)^{3/5} = \underline{5.11 \text{ m}^3/\text{kg}}$$

$$T_2 = 373.15 \times \left( \frac{1.014}{1.985} \right)^{-0.4} = \underline{488.2 \text{ K}}$$

b. From the data we find for  $p_2 = \underline{198.53 \text{ kPa}}$   
 $T_2 = \underline{120^\circ\text{C} = 393.15 \text{ K}}$ .

So the final quality

$$x_2 = \frac{s_1 - (s_f)_2}{(s_{fg})_2} = \frac{4.331 - 1.5275}{5.6013} = 0.5005$$

c. We can estimate the final temperature by using the Clapeyron relation

$$\frac{dT}{dp} = \frac{v_{if}}{s_{if}} = T \frac{v_{if}}{h_{if}} = 933.55 \times \frac{2.625 \times 10^{-5}}{3.73 \times 10^5} = 6.57 \times 10^{-8} \text{ K/Pa}$$

Upon writing  $dT/dp \sim \Delta T/\Delta p$  we find

$$\Delta T \approx \left( \frac{dT}{dp} \right) \Delta p = 6.57 \times 10^{-8} \times 97180 = 0.0064 \text{ K}$$

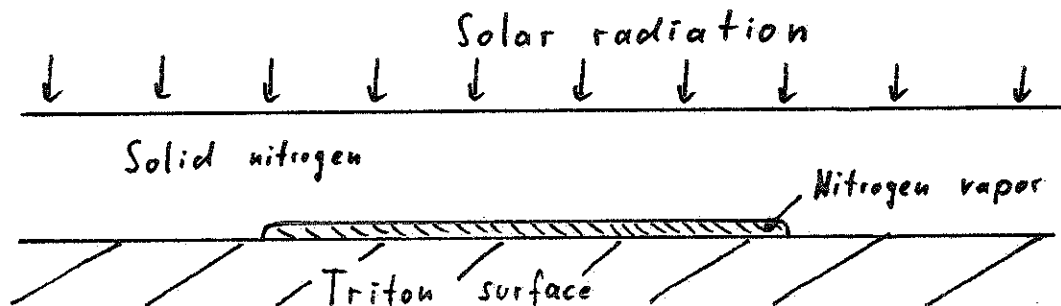
$$\underline{T_2 = T_1 + 0.0064} \quad \text{for } T_1 \text{ in K}$$

## GENERAL THERMODYNAMICS

## Problem Set 9

Due: November 15, 1990

1. Problem ?
2. Problem ?
3. Problem ?
4. As discussed in the attached article, the spacecraft *Voyager 2* observed plumes on the surface of Triton, Neptune's largest moon (See also *Science*, 1990, Vol. 250, pp. 410 - 443). One hypothesis for this phenomenon assumes that the absorption of solar radiation in the solid-nitrogen layer covering the Triton surface leads to the formation of nitrogen vapor pockets. If the vapor pressure in a pocket exceeds the burst pressure of the solid-nitrogen layer, then the vapor is assumed to escape suddenly, thus forming a nitrogen geyser. From other *Voyager 2* measurements, it is known that the outer surface temperature of Triton is approximately 40 K. In the following, we will develop a very simple model for this process, based on the schematic below.



- (a) Show that the sublimation pressure curve, which gives the pressure as a function of temperature for solid-vapor two-phase mixtures in stable equilibrium states, can be approximated by

$$\ln\left(\frac{p}{p_{tp}}\right) \approx \frac{h_{jg}}{R_M} \left(\frac{1}{T_{tp}} - \frac{1}{T}\right)$$

where  $R_M$  is the specific gas constant of the vapor, and  $p_{tp}$  and  $T_{tp}$  are triple point pressure and temperature, respectively. Hint: Start with the Clausius-Clapeyron relation. Neglect terms that are small compared to others. Model the vapor as an ideal gas (a very rough approximation).

- (b) You find thermodynamic properties of nitrogen in Tables B.1, B.2, B.3 and B.13 of the textbook. If the solid and vapor are both at 40 K, what process leads to the vapor formation? Estimate the specific latent heat for this process.
- (c) Based on your result in (b), estimate the vapor production rate, mass per unit time, per unit Triton surface area, if the solar energy flux causing the vapor production is  $0.4 \text{ W/m}^2$  at the Triton surface.
- (d) Using the result in (a), determine the pressure in the vapor pocket if both vapor and solid are in mutual stable equilibrium at 40 K.
- (e) Assume that the burst pressure of the ice layer is  $p_b = 5000 \text{ Pa}$ , and model the vapor as an ideal gas. Starting at the state of part (b), how much vapor must be produced, if the pocket has a diameter of 50 m, and a thickness of 10 cm, to make the ice layer burst? How long will this take?



## Solar-system exploration

## Plume de ma Triton

**P**LANETARY scientists are famous for making little spacecraft go a long way; they can do the same trick with data, too. When *Voyager 2* whipped around Triton, Neptune's largest moon, last summer, it sent back only 100 or so photos, of which a mere handful were close-ups of the surface. Careful inspection showed that those pictures held a big surprise: dark plumes towering 8km above the surface, then being spread out by the jet-stream winds into long thin clouds. Scientists at JPL, the laboratory in Pasadena, California, that ran the *Voyager* programme, excitedly decided that they had found the first extraterrestrial geysers. They were justifiably pleased about finding an explanation for such an oddity. Now they have surpassed themselves, and come up with other possible explanations, as well.

If the plumes are geysers, what drives them? Earthly geysers are powered by heat deep within the earth; but most of the warmth in Triton's rocky core has already been lost. If the heat is not coming from below, perhaps it comes from above—from the sun. Triton's surface is largely covered with frozen nitrogen. A clear layer of frozen

nitrogen a metre or two thick, covering a darker layer—perhaps of hydrocarbons—could act as a greenhouse. Heat could get in but not out. The dark layer warms up and some of the frozen nitrogen turns to gas. That gas then erupts through the ice as a geyser.

Various forms of the geyser hypothesis were recently discussed in *Science*. Some think that the gas erupts at high speed; others that it seeps out but climbs into the sky because it is warmer (and thus lighter) than the atmosphere (which is also nitrogen). Heat and gas may well move around under the insulating ice, allowing a large greenhouse to feed a small geyser, and thus allowing long eruptions. If the nitrogen greenhouse is thicker and has no dark layer below it, it might provide enough heat and pressure for reservoirs of liquid nitrogen, which could lead to particularly violent eruptions. If the moon's internal heat reaches the ice layer unevenly, concentrated at a few hot spots, it too might create such explo-

sive subtritonian lakes.

There is an alternative to geysers. Dr Andrew Ingersoll and Dr Kimberly Tryka, of the California Institute of Technology, suggest that the plumes may be dust-devils, carrying heat and muck into the upper atmosphere. They take their idea from the fact that studies of radio signals from *Voyager*, which passed through Triton's atmosphere, seem to show that it is warmer than the ice of the surface. Dr Ingersoll and Dr Tryka point out that dark iceless spots on the surface can be warmed by the sun, and that cold gas above these spots could form little whirlwinds, just as cold desert air can.

The idea has its charm. Dust devils could stay thin and focused as they rise 8km, whereas jets from geysers might be expected to spread out. They could also provide the heat to warm the atmosphere. Unfortunately many scientists have doubts about the warm atmosphere. They want to do more detailed analyses of the radio data. It is also unclear how winds in an atmosphere as thin as Triton's—100,000 times thinner than the earth's—could lift up the dark substances seen in the plumes.

The solar-powered geysers have their drawbacks, as well. If the frozen nitrogen takes the form of fluffy opaque frost, rather than solid, clear ice, it does not work as a greenhouse. Studies of how nitrogen behaves at very low temperatures and pressures might help to sort that out. Further study of *Voyager*'s meagre messages may also help. The best answer, though, is to take another look. Around 2001 the planets will be arranged so that a probe could be launched into orbit around Neptune, rather than just flying past it as *Voyager* did. It would not get there until about 2014, though—by which time the scientists now poring over the plumes may be past caring.



Thar she blows

## Solution

(a) Clausius - Clapeyron relation

$$\frac{dP}{dT} = \frac{1}{T} \frac{h_g - h_f}{v_g - v_f} \quad (1)$$

Assume  $v_f \approx v_l$ . Assume further that  $v_g \gg v_f$ .

Recall ideal-gas equation of state,

$$pv = R_M T \quad (2)$$

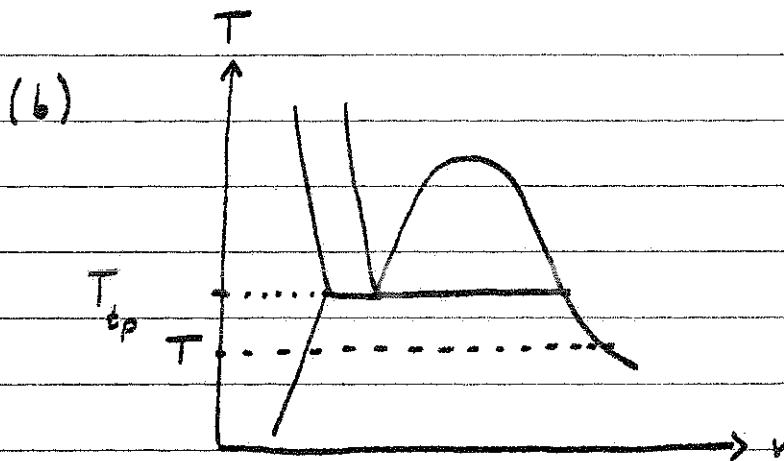
and substitute in (1), to find

$$\frac{dP}{dT} \approx \frac{P h_{fg}}{R_M T^2} \quad (3)$$

and upon integration,

$$\ln \left( \frac{P}{P_{tp}} \right) \approx \frac{h_{fg}}{R_M} \left( \frac{1}{T_{tp}} - \frac{1}{T} \right) \quad (4)$$

q.e.d.



For nitrogen,  $T_{tp} = 63.2 \text{ K}$ , and for  $T < T_{tp}$ ,  
the phase change is a sublimation process.

From Table B.13, in the vicinity of the

triple point,  $h_{fg} = 214.83 \text{ kJ/kg}$ . From Table B.3,

at  $p = 1 \text{ bar}$ ,  $h_{if} = 25.7 \text{ kJ/kg}$ . Assume that

$$h_{if}(p_{tp}) \approx h_{if}(p = 1 \text{ bar}).$$

Recall that in the vicinity of the triple point,

$$h_{ig} = h_{if} + h_{fg}. \quad \text{Hence, } h_{ig} \approx 240.5 \times 10^3 \text{ J/kg}.$$

Assume that for  $T < T_{tp}$ ,  $h_{ig} \neq h_{ig}(T)$ .

(c) The sublimation rate per unit Triptou

$$\text{surface area is } (\dot{m}/A) = \frac{(\dot{E}/A)}{h_{jg}} = \frac{0.4 \text{ W/m}^2}{240.5 \times 10^3 \text{ J/kg}}$$

$$(\dot{m}/A) = 1.66 \times 10^{-6} \text{ kg/s}$$

(d) For nitrogen,  $M = 28.013 \text{ kg/kmol}$ .

$$\text{Hence, } R_M = R/M = 8.3145 \frac{\text{J}}{\text{mol K}} / (28.013 \text{ kg/kmol})$$

$$R_M = 296.8 \frac{\text{J}}{\text{kg K}}$$

From Table B.1,  $P_{tp} = 12.6 \text{ kPa}$

Substitute  $T = 40 \text{ K}$  into equation (4), to find

$$P_{j,\text{sat}}(T = 40 \text{ K}) = 7.43 \text{ Pa}$$

(e) Recall  $pV = m R_M T$

Assume that during the sublimation process,

the system consisting of ice and vapor passes

through stable equilibrium states.

Then the temperature at the burst pressure

is  $T(P_b) = T_{d, \text{sat}}(P_b)$  and can be

calculated from equation (4),

$$T(P_b) = 58.95 \text{ K}$$

At the burst pressure,  $m(P_b) = \frac{P_b V}{R_m T}$

$$= \frac{5000 \text{ Pa} \times \frac{\pi}{4} 2500 \text{ m}^2 \times 0.1 \text{ m}}{296.8 \text{ J/kgK} \times 58.95 \text{ K}}$$

$$= 56.1 \text{ kg}$$

At the initial pressure,  $m(T=40\text{K}) = \frac{7.43 \text{ Pa} \times 196.3 \text{ m}^3}{296.8 \text{ J/kgK} \times 40 \text{ K}}$

$$= 0.123 \text{ kg}$$

The mass of vapor to be generated is  $\Delta m = 55.98 \text{ kg}$

with the sublimation rate of part (c), and an area

of  $A = 1963 \text{ m}^2$ , the time up to the burst is

$$t_b = \frac{\Delta m}{(\dot{m}(A) A)} = \frac{55.98 \text{ kg}}{1.66 \times 10^{-6} \text{ kg/s} \times 1963 \text{ m}^2} = 1.7 \times 10^4 \text{ s} = 4.8 \text{ hours}$$

Note that this simple calculation assumes the volume of the vapor pocket to be constant, which is a very rough assumption

2.451J and 22.571J  
GENERAL THERMODYNAMICS

Problem Set 10

Due November 29, 1990

1. Problem 22.4
2. Problem 22.8
3. Problem 22.9
4. Problem 23.6
5. Problem 23.12

2.451J and 22.571J

GENERAL THERMODYNAMICS

Problem Set 11

Due December 6, 1990

1. Problem 24.3
2. Problem 24.17
3. Problem 24.20
4. Problem 25.6



Monday, December 17, 1990

Time: 1:30–4:30 p.m.

Massachusetts Institute of Technology  
Scheduled Examination in  
General Thermodynamics  
2.451J and 22.571J

Note: Students are not permitted to use any books, notebooks, or papers during the course of this examination. Each student is permitted to have a few-page personal summary of key concepts and formulas.

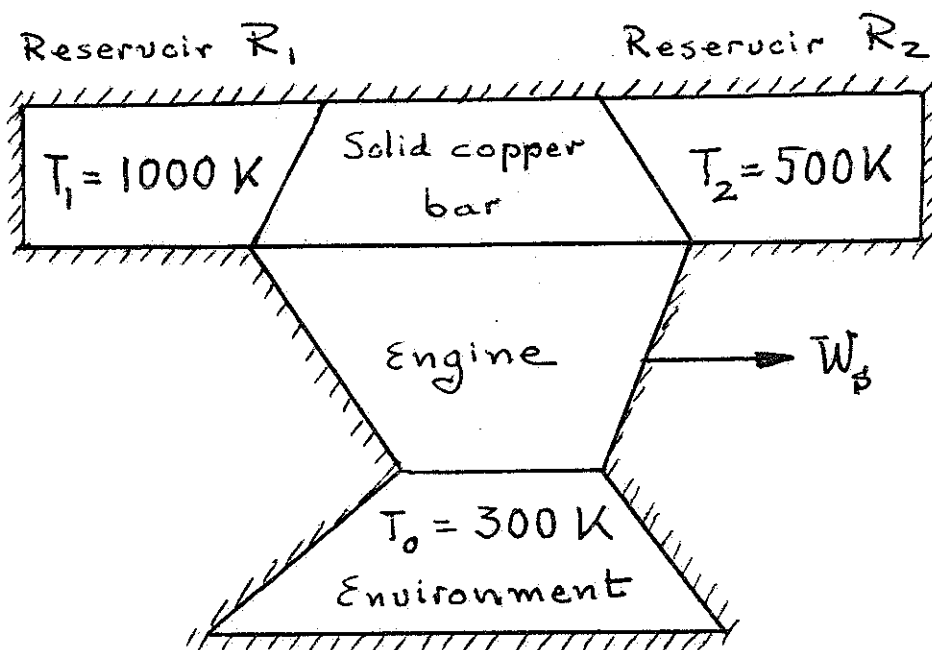
Problem 1 (10/135)

- (5/135) a. Write the first law of thermodynamics.
- (5/135) b. Write the second law of thermodynamics for systems without chemical and nuclear reactions altering the amounts of constituents.

Problem 2 (30/135)

A solid copper bar interacts only with two reservoirs  $R_1$  and  $R_2$  at  $T_1 = 1000$  K and  $T_2 = 500$  K, and a cyclic engine as shown in the sketch. In addition, the engine delivers shaft work to a weight and interacts with the environment at  $T_0 = 300$  K. The energy transfer out of  $R_1$  is  $Q^{R_1 \rightarrow} = 7000$  kJ, the entropies generated by irreversibility in the solid copper bar  $[S_{\text{irr}}]_s = 7$  kJ/K and in the cyclic engine  $[S_{\text{irr}}]_e = 2$  kJ/K. The entropy transfer into  $R_2$  is  $S^{R_2 \leftarrow} = 4$  kJ/K.

- (5/135) a. Find the work equivalent of the energy transfer out of  $R_1$ .
- (15/135) b. Find the work done by the cyclic engine.
- (10/135) c. Find the effectiveness (thermodynamic efficiency) with which  $Q^{R_1 \rightarrow}$  is utilized.



Problem 3 (30/135)

A boiler operates in steady state at a constant pressure of 200 bar and a water flow rate of 100 kg/s. The water enters and leaves the boiler at temperatures of 100 °C and 500 °C, respectively. The boiler experiences a heat interaction at  $T_Q = 1000$  °C, and the temperature of the environment is  $T_0 = 25$  °C. The properties of water at 200 bar are attached.

- (5/135)      a.      What is the rate of heat into the boiler ?
- (15/135)     b.      What is the rate of lost work due to irreversibility ?
- (10/135)     c.      What is the change in the availability rate of the water ?

Properties of H<sub>2</sub>O

$p = 10 \text{ MPa}$							$\dot{p} = 20 \text{ MPa}$						
$T$	$v$	$u$	$h$	$s$	$c_v$	$c_p$	$T$	$v$	$u$	$h$	$s$	$c_v$	$c_p$
$^{\circ}\text{C}$	$\text{m}^3/\text{kg}$	$\text{kJ/kg}$	$\text{kJ/kg}$	$\text{kJ/kgK}$	$\text{kJ/kgK}$	$\text{kJ/kgK}$	$^{\circ}\text{C}$	$\text{m}^3/\text{kg}$	$\text{kJ/kg}$	$\text{kJ/kg}$	$\text{kJ/kgK}$	$\text{kJ/kgK}$	$\text{kJ/kgK}$
0	0.000995	-0.3	9.6	-0.0005	4.163	4.163	0	0.000990	-0.2	19.6	-0.0004	4.128	4.128
50	0.001008	207.4	217.4	0.6983	3.994	4.155	50	0.001003	205.9	226.0	0.6937	3.970	4.134
100	0.001039	415.7	426.0	1.2984	3.759	4.194	100	0.001034	412.9	433.6	1.2909	3.744	4.173
200	0.001148	844.1	855.5	2.3170	3.331	4.447	200	0.001139	837.3	860.0	2.3023	3.320	4.399
Sat. liq.	0.001453	1393.3	1407.8	3.3599	3.098	6.140	300	0.001360	1305.7	1332.8	3.2063	3.052	5.314
311.06	0.01657	1150.5	1316.2	2.2530			Sat. liq.	0.002041	1787.5	1828.3	4.0169	3.439	22.81
Sat. vap.	0.01802	2543.8	2724.0	5.6129	3.048	7.014	365.81	0.003794	505.0	580.9	0.9091		
350	0.02242	2698.6	2922.8	5.9433	2.323	4.022	Sat. vap.	0.005835	2292.5	2409.2	4.9260	4.070	44.68
400	0.02641	2831.8	3095.9	6.2109	1.999	3.082	400	0.009943	2618.6	2817.4	5.5528	2.700	6.327
500	0.03279	3045.2	3373.1	6.5956	1.849	2.589	500	0.01477	2942.2	3237.6	6.1391	2.045	3.274
600	0.03837	3241.2	3624.8	6.9020	1.849	2.470	600	0.01818	3173.4	3537.0	6.5038	1.964	2.808
700	0.04358	3434.2	3870.0	7.1678	1.879	2.442	700	0.02113	3385.9	3808.6	6.7984	1.959	2.646
800	0.04860	3628.5	4114.4	7.4069	1.920	2.450	800	0.02386	3592.2	4069.3	7.0535	1.971	2.579
900	0.05350	3825.8	4360.8	7.6264	1.967	2.479	900	0.02645	3796.9	4325.9	7.2821	1.994	2.559
1000	0.05833	4027.3	4610.6	7.8307	2.017	2.519	1000	0.02897	4002.6	4582.0	7.4916	2.026	2.567

Problem 4 (40/135)

In many chemical processing plants, a hot stream must be cooled and a cold stream must be heated. One method of achieving these two tasks is by having the two streams interact in a heat exchanger. Another is by making the two streams interact via work delivering machinery and, if necessary, allowing the machinery to interact also with the environment at  $T_0 = 293$  K.

Consider: (a) a hot stream of a perfect gas ( $c_p = 1$  kJ/kg K,  $R_M = 0.286$  kJ/kg K) at  $T_{g1} = 750$  K and  $p_{g1} = 60$  atm which must be cooled to  $T_{g2} = 310$  K, and the pressure of which must be reduced to  $p_{g2} = 1$  atm; and (b) a cold stream of water at  $T_{w1} = 20^\circ$  C and  $p_{w1} = 1$  bar which must be transformed to superheated steam at  $T_{w2} = 420^\circ$  C and  $p_{w2} = p_{w1}$ . The required pressure drop of the stream being cooled is achieved by a throttle at the exit of the heat exchanger. Useful properties of water are attached.

- (10/135) a. How much superheated steam can be raised in the heat exchanger per kilogram of gas cooled?
- (15/100) b. If instead of the heat exchanger and throttle, work producing machinery is used, what is the largest amount of work per kilogram of gas cooled as specified, and for raising the same amount of steam as in part (a)?
- (10/100) c. How much entropy is generated by irreversibility in part (a)?
- (5/100) d. What is the effectiveness of the heat exchanger in part (a)?

**Table 4. Liquid**

p (t Sat.)		0				25 (223.99)				50 (263.99)			
t	v	u	h	s	v	u	h	s	v	u	h	s	
Sat.					1.1973	959.1	962.1	2.5546	1.2859	1147.8	1154.2	2.9202	
0	1.0002	-.03	-.03	-.0001	.9990	-.00	2.50	-.0000	.9977	.04	5.04	.0001	
20	1.0018	83.95	83.95	.2966	1.0006	83.80	86.30	.2961	.9995	83.65	88.65	.2956	
40	1.0078	167.56	167.56	.5725	1.0067	167.25	169.77	.5715	1.0056	166.95	171.97	.5705	
60	1.0172	251.12	251.12	.8312	1.0160	250.67	253.21	.8298	1.0149	250.23	255.30	.8285	
80	1.0291	334.87	334.87	1.0753	1.0280	334.29	336.86	1.0737	1.0268	333.72	338.85	1.0720	
100	1.0436	418.96	418.96	1.3069	1.0423	418.24	420.85	1.3050	1.0410	417.52	422.72	1.3030	
120	1.0604	503.57	503.57	1.5278	1.0590	502.68	505.33	1.5255	1.0576	501.80	507.09	1.5233	
140	1.0800	588.89	588.89	1.7395	1.0784	587.82	590.52	1.7369	1.0768	586.76	592.15	1.7343	
160	1.1024	675.19	675.19	1.9434	1.1006	673.90	676.65	1.9404	1.0988	672.62	678.12	1.9375	
180	1.1283	762.72	762.72	2.1410	1.1261	761.16	763.97	2.1375	1.1240	759.63	765.25	2.1341	
200	1.1581	851.8	851.8	2.3334	1.1555	849.9	852.8	2.3294	1.1530	848.1	853.9	2.3255	
210	1.1749	897.1	897.1	2.4281	1.1720	895.0	898.0	2.4238	1.1691	893.0	898.8	2.4195	
220	1.1930	943.0	943.0	2.5221	1.1898	940.7	943.7	2.5174	1.1866	938.4	944.4	2.5128	
230	1.2129	989.6	989.6	2.6157	1.2092	987.0	990.1	2.6105	1.2056	984.5	990.6	2.6055	
240	1.2347	1037.1	1037.1	2.7091	1.2305	1034.2	1037.2	2.7034	1.2264	1031.4	1037.5	2.6979	
250	1.2590	1085.6	1085.6	2.8027	1.2540	1082.3	1085.4	2.7964	1.2493	1079.1	1085.3	2.7902	
260	1.2862	1135.4	1135.4	2.8970	1.2804	1131.6	1134.8	2.8898	1.2749	1127.9	1134.3	2.8830	
270	1.3173	1186.8	1186.8	2.9926	1.3102	1182.4	1185.7	2.9844	1.3036	1178.2	1184.7	2.9766	
280	1.3535	1240.4	1240.4	3.0904	1.3447	1235.1	1238.5	3.0808	1.3365	1230.2	1236.8	3.0717	
290	1.3971	1297.0	1297.0	3.1918	1.3855	1290.5	1294.0	3.1801	1.3750	1284.4	1291.3	3.1693	
300	1.4520	1358.1	1358.1	3.2992	1.4357	1349.6	1353.2	3.2843	1.4214	1341.9	1349.0	3.2708	
310									1.4803	1404.1	1411.5	3.3789	
p (t Sat.)		75 (290.59)				100 (311.06)				125 (327.89)			
t	v	u	h	s	v	u	h	s	v	u	h	s	
Sat.	1.3677	1282.0	1292.2	3.1649	1.4524	1393.0	1407.6	3.3596	1.5466	1492.2	1511.5	3.5286	
0	.9965	.06	7.54	.0002	.9952	.09	10.04	.0002	.9940	.13	12.56	.0003	
20	.9984	83.50	90.99	.2950	.9972	83.36	93.33	.2945	.9961	83.21	95.67	.2940	
40	1.0045	166.64	174.18	.5696	1.0034	166.35	176.38	.5686	1.0024	166.05	178.58	.5676	
60	1.0138	249.79	257.40	.8272	1.0127	249.36	259.49	.8258	1.0116	248.94	261.58	.8245	
80	1.0256	333.15	340.84	1.0704	1.0245	332.59	342.83	1.0688	1.0233	332.03	344.82	1.0672	
100	1.0397	416.81	424.62	1.3011	1.0385	416.12	426.50	1.2992	1.0373	415.42	428.39	1.2973	
120	1.0562	500.94	508.86	1.5211	1.0549	500.08	510.64	1.5189	1.0535	499.24	512.41	1.5167	
140	1.0752	585.72	593.78	1.7317	1.0737	584.68	595.42	1.7292	1.0722	583.66	597.07	1.7267	
160	1.0970	671.37	679.59	1.9346	1.0953	670.13	681.08	1.9317	1.0935	668.91	682.58	1.9288	
180	1.1219	758.13	766.55	2.1308	1.1199	756.65	767.84	2.1275	1.1178	755.19	769.16	2.1242	
200	1.1505	846.3	854.9	2.3216	1.1480	844.5	856.0	2.3178	1.1456	842.8	857.1	2.3141	
210	1.1664	891.0	899.8	2.4154	1.1637	889.1	900.7	2.4113	1.1610	887.1	901.6	2.4073	
220	1.1835	936.2	945.1	2.5083	1.1805	934.1	945.9	2.5039	1.1776	932.0	946.7	2.4995	
230	1.2022	982.1	991.1	2.6006	1.1988	979.7	991.7	2.5958	1.1955	977.4	992.3	2.5911	
240	1.2225	1028.6	1037.8	2.6925	1.2187	1026.0	1038.1	2.6872	1.2150	1023.4	1038.5	2.6821	
250	1.2448	1076.0	1085.3	2.7843	1.2405	1073.0	1085.4	2.7785	1.2363	1070.1	1085.6	2.7729	
260	1.2696	1124.4	1134.0	2.8763	1.2645	1121.1	1133.7	2.8699	1.2597	1117.8	1133.5	2.8637	
270	1.2973	1174.1	1183.9	2.9691	1.2913	1170.3	1183.2	2.9618	1.2857	1166.5	1182.6	2.9548	
280	1.3288	1225.4	1235.4	3.0631	1.3216	1220.9	1234.1	3.0548	1.3148	1216.6	1233.0	3.0469	
290	1.3653	1278.8	1289.0	3.1591	1.3564	1273.4	1287.0	3.1495	1.3481	1268.4	1285.2	3.1404	
300	1.4087	1334.9	1345.4	3.2584	1.3972	1328.4	1342.3	3.2469	1.3867	1322.3	1339.6	3.2361	
310	1.4622	1394.9	1405.8	3.3629	1.4465	1386.6	1401.1	3.3485	1.4326	1379.1	1397.0	3.3353	
320	1.5330	1461.1	1472.6	3.4764	1.5093	1449.8	1464.9	3.4569	1.4895	1439.9	1458.5	3.4399	
330					1.5972	1521.5	1537.5	3.5784	1.5646	1507.1	1526.6	3.5538	
340									1.6795	1586.9	1607.9	3.6874	

1 Bar = 1.01972 kg./sq.cm.: 1 Joule = 1/4.1868 I.T.Cal.

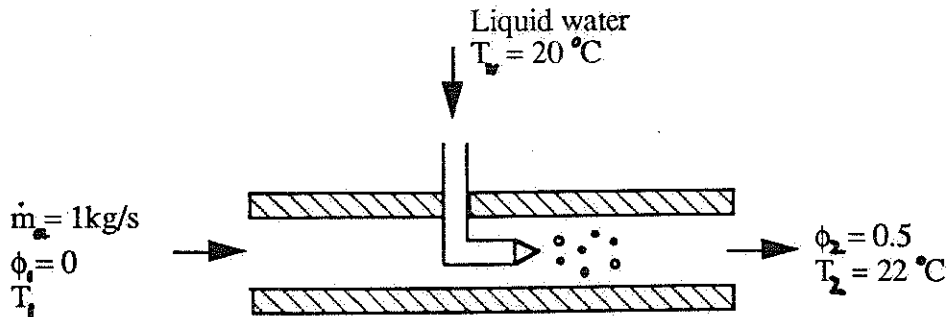
Table 3. Vapor

t	90 (96.71)					95 (98.20)					1.0 (99.63)					1.1 (102.31)					1.2 (104.80)					1.3 (107.13)					p (Sat.)		
	Sat.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29		30	
90	1869.5	2502.6	2670.9	7.3949	1777.3	2504.4	2673.2	7.3767	1694.0	2506.1	2675.5	7.3594	1809.2	2476.4	2707.0	7.0136	1716.0	2472.7	2681.1	7.2713	1428.4	2512.1	2683.5	7.2981	1700.2	2427.7	2663.7	6.9211	1100.2	2427.7	2663.7	6.9211	
95	1610.9	2410.0	2574.9	7.1131	1521.6	2420.1	2574.8	7.0898	1445.0	2426.2	2572.7	7.0633	1532.9	2416.4	2581.2	7.0464	1471.0	2413.0	2567.2	7.3056	1196.0	2424.3	2568.1	7.2978	1218.0	2427.7	2578.9	6.9000	900.0	2427.7	2578.9	6.9000	
100	1333.5	2141.9	2305.7	7.1809	1336.5	2144.9	2305.7	7.1533	1268.4	2146.7	2301.7	7.1274	1336.5	2141.9	2305.7	7.1005	1298.8	2138.0	2291.7	7.3485	1000.0	2144.9	2301.7	7.2985	1020.0	2147.9	2308.7	6.9015	750.0	2147.9	2308.7	6.9015	
105	1093.4	2013.3	2206.1	7.2718	1097.4	2017.7	2206.1	7.2442	1030.8	2019.5	2200.2	7.2186	1097.4	2013.3	2206.1	7.1917	1069.4	2010.0	2191.7	7.4411	800.0	2017.7	2200.2	7.3963	820.0	2020.7	2213.7	6.9030	550.0	2020.7	2213.7	6.9030	
110	922.2	1861.3	2106.6	7.3750	926.2	1865.6	2106.6	7.3474	860.0	1867.3	2101.7	7.3218	926.2	1861.3	2106.6	7.2949	904.8	1858.0	2091.7	7.5886	600.0	1865.6	2101.7	7.5429	620.0	1868.6	2114.7	6.9045	350.0	2114.7	2114.7	6.9045	
115	780.0	1730.9	2006.6	7.4821	784.0	1735.2	2006.6	7.4545	720.0	1741.9	2001.7	7.4289	784.0	1730.9	2006.6	7.4020	763.8	1732.0	1991.7	7.8311	450.0	1741.9	2001.7	7.7860	470.0	1744.9	2008.7	6.9060	200.0	2008.7	2008.7	6.9060	
120	660.0	1610.0	1906.6	7.5932	664.0	1614.3	1906.6	7.5656	600.0	1620.1	1901.7	7.5400	664.0	1610.0	1906.6	7.5131	647.8	1601.0	1891.7	8.2733	300.0	1620.1	1901.7	8.2272	320.0	1623.0	1908.7	6.9075	50.0	1908.7	1908.7	6.9075	
125	560.0	1500.0	1806.6	7.7044	564.0	1504.3	1806.6	7.6768	500.0	1510.1	1801.7	7.6512	564.0	1500.0	1806.6	7.6243	551.8	1491.0	1791.7	8.5664	150.0	1510.1	1801.7	8.5203	170.0	1512.0	1808.7	6.9090	0.0	1808.7	1808.7	6.9090	
130	480.0	1400.0	1706.6	7.8156	484.0	1404.3	1706.6	7.7880	420.0	1410.1	1701.7	7.7624	484.0	1400.0	1706.6	7.7349	471.8	1391.0	1691.7	9.4550	0.0	1410.1	1701.7	9.4089	0.0	1412.0	1708.7	6.9105	0.0	1708.7	1708.7	6.9105	
135	410.0	1300.0	1606.6	7.9268	414.0	1304.3	1606.6	7.8992	360.0	1310.1	1601.7	7.8736	414.0	1300.0	1606.6	7.8461	405.8	1291.0	1591.7	10.3440	0.0	1310.1	1601.7	10.2975	0.0	1312.0	1608.7	6.9120	0.0	1608.7	1608.7	6.9120	
140	350.0	1200.0	1506.6	8.0380	354.0	1204.3	1506.6	8.0104	300.0	1210.1	1501.7	7.9848	354.0	1200.0	1506.6	7.9573	345.8	1191.0	1491.7	11.2330	0.0	1210.1	1501.7	11.1865	0.0	1212.0	1508.7	6.9135	0.0	1508.7	1508.7	6.9135	
145	300.0	1100.0	1406.6	8.1492	304.0	1104.3	1406.6	8.1216	260.0	1110.1	1401.7	8.0960	304.0	1100.0	1406.6	8.0685	300.8	1091.0	1391.7	12.1220	0.0	1110.1	1401.7	12.0745	0.0	1112.0	1408.7	6.9150	0.0	1408.7	1408.7	6.9150	
150	260.0	1000.0	1306.6	8.2604	264.0	1004.3	1306.6	8.2328	220.0	1010.1	1301.7	8.2072	264.0	1000.0	1306.6	8.1797	260.8	991.0	1291.7	13.0110	0.0	1010.1	1301.7	12.9667	0.0	1012.0	1308.7	6.9165	0.0	1308.7	1308.7	6.9165	
155	220.0	900.0	1206.6	8.3716	224.0	904.3	1206.6	8.3440	180.0	910.1	1201.7	8.3184	224.0	900.0	1206.6	8.2857	220.8	891.0	1191.7	13.8990	0.0	910.1	1201.7	13.8465	0.0	912.0	1208.7	6.9180	0.0	1208.7	1208.7	6.9180	
160	180.0	800.0	1106.6	8.4828	184.0	804.3	1106.6	8.4552	140.0	810.1	1101.7	8.4296	184.0	800.0	1106.6	8.3913	180.8	791.0	1091.7	14.7870	0.0	810.1	1101.7	14.7315	0.0	812.0	1108.7	6.9195	0.0	1108.7	1108.7	6.9195	
165	150.0	700.0	1006.6	8.5940	154.0	704.3	1006.6	8.5664	100.0	710.1	1001.7	8.5408	154.0	700.0	1006.6	8.5125	150.8	691.0	991.7	15.6750	0.0	710.1	1001.7	15.6145	0.0	712.0	1008.7	6.9210	0.0	1008.7	1008.7	6.9210	
170	120.0	600.0	906.6	8.7052	124.0	604.3	906.6	8.6776	60.0	610.1	901.7	8.6520	124.0	600.0	906.6	8.6087	120.8	591.0	891.7	16.5630	0.0	610.1	901.7	16.5015	0.0	612.0	908.7	6.9225	0.0	908.7	908.7	6.9225	
175	100.0	500.0	806.6	8.8164	104.0	504.3	806.6	8.7888	40.0	510.1	801.7	8.7632	104.0	500.0	806.6	8.7197	100.8	491.0	791.7	17.4510	0.0	510.1	801.7	17.3845	0.0	512.0	808.7	6.9240	0.0	808.7	808.7	6.9240	
180	80.0	400.0	706.6	8.9276	84.0	404.3	706.6	8.8992	20.0	410.1	701.7	8.8736	84.0	400.0	706.6	8.8205	80.8	391.0	691.7	18.3390	0.0	410.1	701.7	18.2715	0.0	412.0	708.7	6.9255	0.0	708.7	708.7	6.9255	
185	60.0	300.0	606.6	9.0388	64.0	304.3	606.6	9.0112	0.0	310.1	601.7	8.9856	64.0	300.0	606.6	8.9363	60.8	291.0	591.7	19.2270	0.0	310.1	601.7	19.1545	0.0	312.0	608.7	6.9270	0.0	608.7	608.7	6.9270	
190	40.0	200.0	506.6	9.1500	44.0	204.3	506.6	9.1224	0.0	210.1	501.7	9.0904	44.0	200.0	506.6	9.0411	40.8	191.0	491.7	20.1150	0.0	210.1	501.7	20.0375	0.0	212.0	508.7	6.9285	0.0	508.7	508.7	6.9285	
195	20.0	100.0	406.6	9.2612	24.0	104.3	406.6	9.2336	0.0	110.1	401.7	9.2024	24.0	100.0	406.6	9.1531	20.8	91.0	391.7	21.0030	0.0	110.1	401.7	20.8445	0.0	112.0	408.7	6.9300	0.0	408.7	408.7	6.9300	
200	10.0	0.0	306.6	9.3724	14.0	0.0	306.6	9.3448	0.0	0.0	301.7	9.3144	14.0	0.0	306.6	9.2637	10.8	81.0	291.7	22.0910	0.0	0.0	301.7	21.9315	0.0	0.0	308.7	6.9315	0.0	308.7	308.7	6.9315	
205	0.0	0.0	206.6	9.4836	4.0	0.0	206.6	9.4560	0.0	0.0	201.7	9.4240	4.0	0.0	206.6	9.3729	0.8	71.0	201.7	23.1770	0.0	0.0	201.7	20.9185	0.0	0.0	208.7	6.9330	0.0	208.7	208.7	6.9330	
210	0.0	0.0	106.6	9.5948	0.0	0.0	106.6	9.5672	0.0	0.0	101.7	9.5320	0.0	0.0	106.6	9.4821	0.6	61.0	101.7	24.2630	0.0	0.0	101.7	20.0045	0.0	0.0	108.7	6.9345	0.0	108.7	108.7	6.9345	
215	0.0	0.0	0.0	9.7060	0.0	0.0	0.0	9.6784	0.0	0.0	0.0	9.6432	0.0	0.0	0.0	9.5971	0.4	51.0	0.0	25.3490	0.0	0.0	0.0	19.0905	0.0	0.0	0.0	6.9360	0.0	0.0	0.0	6.9360	
220	0.0	0.0	0.0	9.8172	0.0	0.0	0.0	9.7896	0.0	0.0	0.0	9.7544	0.0	0.0	0.0	9.7033	0.2	41.0	0.0	20.4840	0.0	0.0	0.0	18.1765	0.0	0.0	0.0	6.9375	0.0	0.0	0.0	6.9375	
225	0.0	0.0	0.0	9.9284	0.0	0.0	0.0	9.8992	0.0	0.0	0.0	9.8640	0.0	0.0	0.0	9.8129	0.0	31.0	0.0	15.5690	0.0	0.0	0.0	17.2625	0.0	0.0	0.0	6.9390	0.0	0.0	0.0	6.9390	
230	0.0	0.0	0.0	10.0396	0.0	0.0	0.0	10.0104	0.0	0.0	0.0	9.9752	0.0	0.0	0.0	9.9241	0.0	21.0	0.0	10.6540	0.0	0.0	0.0	16.3485	0.0	0.0	0.0	6.9405	0.0	0.0	0.0	6.9405	
235	0.0	0.0	0.0	10.1508	0.0	0.0	0.0	10.1216	0.0	0.0	0.0	10.0864	0.0	0.0	0.0	10.0353	0.0	11.0	0.0	0.0	0.0	0.0	0.0	15.4345	0.0	0.0	0.0	6.9420	0.0	0.0	0.0	6.9420	
240	0.0	0.0	0.0	10.2620	0.0	0.0	0.0	10.2328	0.0	0.0	0.0	10.1976	0.0	0.0	0.0	10.1465	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	14.5205	0.0	0.0	0.0	6.9435	0.0	0.0	0.0	6.9435
245	0.0	0.0	0.0	10.3732	0.0	0.0	0.0	10.3440	0.0	0.0	0.0	10.3088	0.0	0.0	0.0	10.2577	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	13.6065	0.0	0.0	0.0	6.9450	0.0	0.0	0.0	6.9450
250	0.0	0.0	0.0	10.4844	0.0	0.0	0.0	1																									



Problem 5 (25/135)

The air in Boston is not only very humid in the summer, but also very dry in the winter. Hence, humidifiers are sold, one type of which is depicted in the figure.



Air is entering the well-insulated humidifier at a relative humidity of 0 %. Liquid water at a temperature of  $20^\circ\text{C}$  is added to the air flow. The air leaving the humidifier has a relative humidity of 50 % and a temperature of  $22^\circ\text{C}$ . The streams entering and leaving the humidifier are at a pressure of 1 bar. The air and the water vapor can be modeled as perfect gases. At constant pressure, the specific heat of dry air  $c_{p,a} = 1 \text{ kJ/kg K}$  and that of water vapor  $c_{p,v} = 1.86 \text{ kJ/kgK}$ . The molecular weights of dry air and water vapor are 29 kg/kmol and 18 kg/kmol, respectively. The liquid water behaves as an incompressible liquid ( $dh = c dT$ ) with  $c = 4.19 \text{ kJ/kg K}$ . The properties of saturated water are attached.

(10/135) a. What is the liquid water flow rate ?

(15/135) b. What is the temperature of the entering air ?

TABLE B.14. Values of properties of water, H<sub>2</sub>O.<sup>a</sup>  
Properties of saturated H<sub>2</sub>O

<i>T</i>	<i>p</i>	<i>v<sub>f</sub></i>	<i>v<sub>g</sub></i>	<i>u<sub>f</sub></i>	<i>u<sub>gf</sub></i>	<i>u<sub>g</sub></i>	<i>h<sub>f</sub></i>	<i>h<sub>fg</sub></i>	<i>h<sub>g</sub></i>	<i>s<sub>f</sub></i>	<i>s<sub>fg</sub></i>	<i>s<sub>g</sub></i>
°C	kPa	m <sup>3</sup> /kg		kJ/kg			kJ/kg			kJ/kg K		
0.01	0.61133	0.0009997	206.14	0.0	2374.9	2374.9	0.0	2500.9	2500.9	0.0	9.1555	9.1555
5	0.87210	0.0009999	147.12	20.4	2361.4	2381.8	20.4	2489.7	2510.1	0.0741	8.9508	9.0249
10	1.2276	0.0010004	106.38	41.1	2347.6	2388.7	41.1	2478.2	2519.3	0.1478	8.7522	8.9000
15	1.7051	0.0010011	77.926	62.0	2333.6	2395.6	62.0	2466.5	2528.5	0.2207	8.5598	8.7806
20	2.3385	0.0010021	57.791	82.9	2319.6	2402.5	82.9	2454.7	2537.6	0.2928	8.3736	8.6664
25	3.1691	0.0010032	43.360	103.9	2305.4	2409.3	103.9	2442.8	2546.7	0.3640	8.1932	8.5571
30	4.2460	0.0010046	32.894	125.0	2291.1	2416.1	125.0	2430.8	2555.8	0.4341	8.0184	8.4525
35	5.6280	0.0010062	25.216	146.1	2276.8	2422.9	146.1	2418.7	2564.8	0.5032	7.8491	8.3523
40	7.3836	0.0010080	19.523	167.3	2262.4	2429.7	167.3	2406.6	2573.8	0.5712	7.6850	8.2562
45	9.5932	0.0010100	15.258	188.4	2248.0	2436.4	188.4	2394.4	2582.7	0.6381	7.5259	8.1640
50	12.349	0.0010121	12.032	209.5	2233.5	2443.0	209.5	2382.1	2591.6	0.7039	7.3716	8.0755
60	19.940	0.0010170	7.6710	251.6	2204.6	2456.2	251.6	2357.5	2609.1	0.8323	7.0764	7.9088
70	31.188	0.0010227	5.0422	293.7	2175.4	2469.1	293.7	2332.7	2626.4	0.9567	6.7978	7.7545
80	47.389	0.0010289	3.4072	335.6	2146.1	2481.7	335.7	2307.5	2643.2	1.0772	6.5342	7.6114
90	70.138	0.0010359	2.3606	377.5	2116.6	2494.1	377.6	2282.1	2659.6	1.1942	6.2841	7.4782
100	101.35	0.0010434	1.6729	419.4	2086.6	2506.1	419.5	2256.1	2675.6	1.3080	6.0460	7.3540
110	143.27	0.0010516	1.2102	461.4	2056.3	2517.6	461.5	2229.5	2691.0	1.4189	5.8189	7.2379
120	198.53	0.0010604	0.89186	503.5	2025.3	2528.8	503.7	2202.1	2705.8	1.5275	5.6013	7.1288
130	270.09	0.0010699	0.66851	545.8	1993.6	2539.4	546.1	2173.9	2720.0	1.6338	5.3923	7.0261
140	361.29	0.0010800	0.50885	588.4	1961.2	2549.6	588.8	2144.6	2733.4	1.7381	5.1910	6.9291
150	475.84	0.0010907	0.39278	631.2	1927.8	2559.1	631.8	2114.2	2746.0	1.8406	4.9964	6.8370
160	617.82	0.0011022	0.30706	674.4	1893.5	2567.9	675.1	2082.5	2757.6	1.9415	4.8079	6.7493
170	791.66	0.0011144	0.24282	718.0	1858.0	2576.0	718.8	2049.4	2768.2	2.0409	4.6246	6.6655
180	1002.1	0.0011275	0.19404	761.8	1821.4	2583.2	763.0	2014.7	2777.7	2.1388	4.4461	6.5849
190	1254.4	0.0011414	0.15653	806.1	1783.5	2589.5	807.5	1978.4	2785.9	2.2354	4.2716	6.5070
200	1553.8	0.0011564	0.12735	850.7	1744.1	2594.8	852.5	1940.2	2792.7	2.3308	4.1006	6.4314
210	1906.2	0.0011724	0.10441	895.7	1703.3	2599.0	897.9	1900.1	2798.0	2.4249	3.9326	6.3576
220	2317.8	0.0011897	0.086186	941.1	1660.7	2601.9	943.9	1857.7	2801.6	2.5181	3.7671	6.2852
230	2794.8	0.0012084	0.071577	987.1	1616.3	2603.4	990.4	1813.0	2803.4	2.6104	3.6033	6.2137
240	3344.2	0.0012287	0.059760	1033.5	1569.9	2603.4	1037.7	1765.6	2803.3	2.7020	3.4408	6.1428
250	3972.9	0.0012509	0.050123	1080.7	1521.1	2601.8	1085.7	1715.3	2801.0	2.7932	3.2788	6.0720
260	4688.5	0.0012753	0.042202	1128.7	1469.8	2598.5	1134.7	1661.6	2796.3	2.8843	3.1167	6.0009
270	5498.6	0.0013023	0.035641	1177.7	1415.4	2593.1	1184.8	1604.3	2789.1	2.9755	2.9536	5.9291
280	6411.6	0.0013323	0.030168	1227.8	1357.7	2585.5	1236.3	1542.6	2778.9	3.0672	2.7888	5.8566
290	7435.9	0.0013659	0.025568	1279.3	1296.1	2575.4	1289.4	1476.1	2765.5	3.1599	2.6212	5.7811
300	8580.9	0.0014040	0.021673	1332.3	1230.0	2562.4	1344.4	1403.9	2748.3	3.2539	2.4495	5.7034
310	9856.4	0.0014479	0.018349	1387.3	1158.5	2545.8	1401.6	1325.0	2726.6	3.3496	2.2722	5.6219
320	11274	0.0014991	0.015486	1444.6	1080.3	2524.9	1461.5	1237.9	2699.4	3.4479	2.0871	5.5350
330	12845	0.0015606	0.012996	1504.9	993.4	2498.3	1524.9	1140.3	2665.2	3.5499	1.8906	5.4405
340	14586	0.0016373	0.010797	1569.3	894.6	2463.9	1593.2	1028.2	2621.4	3.6576	1.6769	5.3344
350	16513	0.0017396	0.0088132	1640.5	777.2	2417.8	1669.3	894.0	2563.3	3.7754	1.4347	5.2101
360	18651	0.0018942	0.0069457	1725.0	625.9	2350.9	1760.4	720.1	2480.4	3.9142	1.1373	5.0515
370	21027	0.0022178	0.0049282	1847.9	380.3	2228.1	1894.5	437.2	2331.7	4.1167	0.6798	4.7965
374.14	22089	0.0031550	0.0031550	2029.1	0.0	2029.1	2098.8	0.0	2098.8	4.4289	0.0000	4.4289

<sup>a</sup>Data generated using the correlations in W. C. Reynolds, *Thermodynamic Properties in SI*, Dept. of Mech. Eng., Stanford University, Stanford, CA, 1979.

12/17/90

2.451J and 22.571J

Solution Final Examination

Problem 1

- a. Any two states of a system may always be the end states of a weight process, that is, the initial and final states of a change of state that involves no net effects external to the system except the change in elevation between  $z_1$  and  $z_2$  of a weight. Moreover, for a given weight, the value of the quantity  $Mg(z_1 - z_2)$  is fixed by the end states of the system, and independent of the details of the weight process, where  $M$  is the mass of the weight and  $g$  the gravitational acceleration.
- b. Among all the states of a system with a given value of the energy, and given values of the amounts of constituents and the parameters, there exists one and only one stable equilibrium state. Moreover, starting from any state of a system it is always possible to reach a stable equilibrium state with arbitrarily specified values of amounts of constituents and parameters by means of a reversible weight process.

## Problem 2

a.  $W_{eq} = \left(1 - \frac{T_0}{T_1}\right) Q^{R_1 \rightarrow} = \left(1 - \frac{300}{1000}\right) \times 7000 = 4900 \text{ kJ.}$

b. The energy into reservoir  $R_2$  is given by

$$Q^{R_2 \leftarrow} = T_2 S^{R_2 \leftarrow} = 500 \times 4 = 2000 \text{ kJ}$$

The entropy into the environment is given by

$$S^{e \leftarrow} = \frac{Q^{R_1 \rightarrow}}{T_1} - \frac{Q^{R_2 \leftarrow}}{T_2} + (S_{irr})_s + (S_{irr})_e$$

$$= 7 - 4 + 7 + 2 = 12 \text{ kJ/K}$$

It follows that the energy into the environment

$$Q^{e \leftarrow} = T_0 S^{e \leftarrow} = 300 \times 12 = 3600 \text{ kJ}$$

and so the energy balance for the engine yields

$$\begin{aligned} W_S^{\rightarrow} &= Q^{R_1 \rightarrow} - Q^{R_2 \leftarrow} - Q^{e \leftarrow} = 7000 - 2000 - 3600 \\ &= \underline{1400 \text{ kJ}} \end{aligned}$$

c. The work equivalent of the heat into  $R_2$  is

$$W^{R_2 \leftarrow} = \left(1 - \frac{T_0}{T_2}\right) \times Q^{R_2 \leftarrow} = \left(1 - \frac{300}{500}\right) \times 2000 = 800 \text{ kJ}$$

So the effectiveness is

$$\epsilon = (1400 + 800) / 4900 = \underline{44.9\%}$$

Solution Problem 3

a.  $\dot{Q}^{\leftarrow} = \dot{m} (h_2 - h_1) = 100 \frac{\text{kg}}{\text{s}} (3237.6 - 433.6) \frac{\text{kJ}}{\text{kg}}$

$h_2 = 3237.6 \text{ kJ/kg}$

$h_1 = 433.6 \text{ kJ/kg}$

$\dot{Q}^{\leftarrow} = 280.4 \text{ MW}$  ✗

b. Entropy balance  $0 = \dot{m} (s_1 - s_2) + \frac{\dot{Q}^{\leftarrow}}{T_Q} + \dot{S}_{\text{irr}}$

$\dot{S}_{\text{irr}} = \dot{m} (s_2 - s_1) - \frac{\dot{Q}^{\leftarrow}}{T_Q} = 264.6 \frac{\text{kW}}{\text{K}}$

$s_2 = 6.1331 \text{ kJ/kg K}$

$s_1 = 1.2903 \text{ kJ/kg K}$

Lost work rate  $\Delta \dot{W}^{\rightarrow} = T_0 \dot{S}_{\text{irr}} = 78.84 \text{ MW}$

c. Change in availability rate  $= \dot{m} \Delta (h - T_0 s)$

$= 135.9 \text{ MW}$  ✓

## Problem 4

a. The energy balance for the heat exchanger yields

$$c_p (T_{g1} - T_{g2}) = m_w (h_{w2} - h_{w1})$$

For liquid water at  $T_{w1} = 20^\circ\text{C}$  and  $p_{w1} = 1 \text{ bar}$

$$h_{w1} = 83.95 + (86.30 - 83.95) / 25 = \overset{84.04}{\cancel{86.4}} \text{ kJ/kg}$$

$$s_{w1} \cong 0.2966 \text{ kJ/kg K}$$

For steam at  $420^\circ\text{C}$  and  $1 \text{ bar}$

$$h_{w2} = 3319.6 \text{ kJ/kg}$$

$$s_{w2} = 8.6042 \text{ kJ/kg K}$$

So

$$m_w = 1 \times (750 - 310) / (3319.6 - 86.4) = \underline{0.136} \frac{\text{kg steam}}{\text{kg gas}}$$

b. The change in availability of the gas is

$$W_{\text{largest}}^{\rightarrow} = c_p (T_{g1} - T_{g2}) - T_0 \left[ c_p \ln \frac{T_{g1}}{T_{g2}} - R_m \ln \frac{p_{g1}}{p_{g2}} \right]$$

$$= 440 - 293 \left[ \ln \frac{750}{310} - 0.286 \ln 60 \right]$$

$$= \underline{524.38} \text{ kJ/kg gas.}$$

The change in availability of the water

$$W_{\text{least}}^{\leftarrow} = m_w \left[ h_{w2} - h_{w1} - T_0 (s_{w2} - s_{w1}) \right] = \underline{122.27} \text{ kJ/kg gas}$$

$$s_o \quad W^{\rightarrow} = 524.38 - 122.27 = \underline{402.11} \text{ kJ/kg gas}$$

$$c. \quad \dot{S}_{irr} = W^{\rightarrow} / T_o = 402.11 / 293 = \underline{1.37} \frac{\text{kJ}}{\text{K kg gas}}$$

$$d. \quad \epsilon = 122.27 / 524.38 = \underline{23.3\%}$$

## Solution Problem 5

a. Mass balance

$$\dot{m}_w = \dot{m}_a \omega_2$$

$$\omega = 0.622 \frac{\phi}{P / P_{\text{sat}}(T) - \phi}$$

$$P = 1 \text{ bar}; \quad P_{\text{sat}}(T = 22^\circ\text{C}) = 2.6707 \text{ kPa}$$

$$\omega_2 = 0.008418 \quad \rightarrow \quad \dot{m}_w = \underline{8.418 \text{ g/s}}$$

b. Energy balance

$$\dot{m}_a h_{a,1} + \dot{m}_w h_w = \dot{m}_a (h_{a,2} + \omega_2 h_{v,2})$$

If the enthalpy of liquid water at  $0^\circ\text{C}$  is set equal to zero, then

$$h_w = c T_w$$

$$h_{v,2} = h_{fg}(T=0^\circ\text{C}) + c_{p,v} T_2$$

$$h_{a,1} = c_{p,a} T_1; \quad h_{a,2} = c_{p,a} T_2$$

$$T_1 = T_2 + \frac{\omega_2}{c_{p,a}} \left( h_{fg}(T=0^\circ\text{C}) + c_{p,v} T_2 - c T_w \right)$$

$$\underline{T_1 = 42.03^\circ\text{C}}$$



## Problem 1

An amount of  $4 \times 10^{-7}$  kmol of helium gas is enclosed in the cylinder shown in the figure. The massless piston can move without friction in the cylinder between elevations  $H_L = 0.05$  m and  $H_H = 0.5$  m.

Piston and cylinder are well insulated. The gas in the cylinder can be heated by an electric heater, and it can be stirred by a paddle wheel.

The mass of the weight is  $M_w = 1$  kg, and the piston diameter is  $D = 0.1$  m. Vacuum prevails on the outside of the cylinder.

- Define carefully a system  $A$  whose only constituent is the helium gas.
- In state 1, the piston is at a position  $H_1$  with  $H_L < H_1 < H_H$  and is at rest. What kind of state is state 1?
- State 2 of system  $A$  is reached from state 1 by supplying an energy of  $1.16$  J to the gas through the electric heater, with  $H_L < H_2 < H_H$ . Is the process  $1 \rightarrow 2$  a weight process?

(d) State 3 of system A is reached from state 1 by supplying an energy of 1.16 J to the gas through the paddle wheel, with  $H_3 = H_2$ . Are states 2 and 3 identical?

(e) Is the process  $1 \rightarrow 3$  a weight process?

(f) If  $H_2 - H_1 = 0.0474 \text{ m}$ , what is the difference in the energies of system A in states 1 and 2,  $E_2^A - E_1^A$ ?

(g) System A is modified such that the piston can be pinned in place at any position. In state 3 the piston is pinned in place. Energy is delivered to system A in the amount of 5 J through the paddle wheel to bring the system to state 4. For the composite system consisting of system A, the piston and the weight, what kind of state is state 4? Explain your answer.

